

Fukuoka International Conference on Arithmetic Geometry 2017

Date April 17 (Mon) – 21 (Fri), 2017

Place Nishijin Plaza, Fukuoka, JAPAN

Main Conference Room A

Organizer Shinichi Kobayashi (Kyushu University), Nobuo Tsuzuki (Tohoku University)

This conference is supported by JSPS, Program for Advancing Strategic International Networks to Accelerate the Circulation of Talented Researchers.

Program

April 17 (Mon)

- 9:00 – 10:00 Registration/Opening
- 10:00 – 11:00 Atsushi Shiho (Tokyo University)
Comparison of relatively unipotent log de Rham fundamental groups
- 11:15 – 12:15 Tomoki Mihara (Tokyo Institute of Technology)
On Schikhof Dual of p -adic Formal Groups
- 14:30 – 15:30 Ming-Lun Hsieh (Academia Sinica)
 p -adic L-functions for triple product and applications
- 16:00 – 17:00 Shinichi Kobayashi (Kyushu University)
The p -adic Gross-Zagier formula for higher weight modular forms at non-ordinary primes
- 17:00 – 18:00 Free discussion

April 18 (Tue)

- 10:00 – 11:00 Masanobu Kaneko (Kyushu University)
Finite multiple zeta values
- 11:15 – 12:15 Shuji Yamamoto (Keio University)
Kawashima functions and multiple zeta values
- 14:30 – 15:30 Shun Ohkubo (Nagoya University)
On the rationality of the logarithmic growth filtration of solutions of p -adic differential equations
- 16:00 – 17:00 Jeng-Daw Yu (National Taiwan University)
Recent developments in irregular Hodge filtrations
- 17:00 – 18:00 Free discussion

April 19 (Wed)

- 9:30 – 10:30 Tomoyuki Abe (IPMU)
Existence of crystalline companion and l -adic companion
- 10:45 – 11:45 Bruno Chiarellotto (Padova University)
 l -independence over local function fields
- 14:00 – 18:00 Free discussion

April 20 (Thu)

- 10:00 – 11:00 Takeshi Saito (Tokyo University)
Characteristic cycle of an l -adic sheaf
- 11:15 – 12:15 Andreas Langer (Exeter University)
 p -adic deformation of motivic Chow groups
- 14:30 – 15:30 Shusuke Otabe (Tohoku University)
On a purely inseparable analogue of the Abhyankar conjecture for affine curves
- 16:00 – 17:00 Masataka Chida (Tohoku University)
Chow-Heengger cycles on products of CM elliptic curves.
- 17:00 – 18:00 Free discussion

April 21 (Fri)

- 10:00 – 11:00 Kazuki Yamada (Keio University)
Category of mixed plectic Hodge structures
- 11:15 – 12:15 Jan Nekovář (Paris 6 University)
Some remarks on arithmetic local constants
- 14:30 – 15:30 Shin Hattori (Kyushu University)
Irreducible components of the eigencurve of finite degree are finite over the weight space
- 16:00 – 17:00 Nobuo Tsuzuki (Tohoku University)
On constancy of Newton polygons of F -isocrystals on Abelian varieties
- 17:00 – 18:00 Free discussion

Title and abstract

Speaker: Tomoyuki Abe

Title: Existence of crystalline companion and l -adic companion

Abstract: We will show that there exists a correspondence between smooth l -adic sheaves and overconvergent F -isocrystals over a curve preserving the Frobenius eigenvalues. Moreover, we show the existence of l -adic companions associated to overconvergent F -isocrystals for smooth varieties. Some part of the work is done jointly with Esnault.

Speaker: Bruno Chiarellotto

Title: ℓ -independence over local function fields

Abstract: We study various forms of ℓ -independence (including $\ell = p$) for the cohomology and fundamental groups of varieties on equicharacteristic local fields. Joint work with C. Lazda.

Speaker: Masataka Chida

Title: Chow-Heenger cycles on products of CM elliptic curves

Abstract: Bertolini-Darmon-Prasanna introduced a construction of rational points on CM elliptic curves assuming Tate conjecture for (generalized) Kuga-Sato varieties. In this talk, we will extend their construction to the case of self products of CM elliptic curves. Moreover we will obtain a relation between the p -adic Abel-Jacobi image of the cycles and the special values of (p -adic) L -functions generalizing their works.

Speaker: Shin Hattori

Title: Irreducible components of the eigencurve of finite degree are finite over the weight space

Abstract: Let p be a rational prime and N a positive integer prime to p . The Coleman-Mazur eigencurve C_N is a rigid analytic curve over \mathbb{Q}_p which p -adically interpolates the set of classical elliptic eigenforms of finite slope and tame level N . In this talk, I will explain a joint work with James Newton in which we show that any irreducible component of C_N of finite degree over the weight space W is actually finite over W . By a theorem of Chenevier, our theorem plus a conjecture on slopes near the boundary of W (due to Coleman-Mazur, Buzzard-Kilford) implies that any such component should be in the ordinary locus.

Speaker: Ming-Lun Hsieh

Title: p -adic L -functions for triple product and applications

Abstract: In this talk, we present a construction of p -adic triple product L -functions for Hida families with explicit interpolation formulae. Arithmetic applications to anticyclotomic p -adic L -functions for modular forms will be discussed

Speaker: Masanobu Kaneko

Title: Finite multiple zeta values

Abstract: We discuss two very different “finite” versions of the classical multiple zeta values. After giving some basics, we present a conjectural isomorphism of the two rings of finite multiple zeta values and give some results which support our conjecture. This is a joint work with Don Zagier.

Speaker: Shinichi Kobayashi

Title: The p -adic Gross-Zagier formula for higher weight modular forms at non-ordinary primes

Abstract: We explain the higher weight generalization of the p -adic Gross-Zagier formula for elliptic curves at non-ordinary primes obtained by the speaker before. It is also the non-ordinary generalization of the same formula obtained by J. Nekovář at ordinary primes.

Speaker: Andreas Langer

Title: p -adic deformation of motivic Chow groups

Abstract: For a smooth projective scheme Y over $W(k)$ we consider an element in the motivic Chow group of the reduction Y_m over the truncated Witt ring $W_m(k)$ and give a “Hodge” criterion using the crystalline cycle class in relative crystalline cohomology for the element to lift to the continuous Chow group of Y . The result extends previous work of Bloch-Esnault-Kerz on the p -adic variational Hodge conjecture to a relative setting. In the course of the proof we derive two new results on the relative de Rham-Witt complex and its Nygaard filtration, and work with relative syntomic complexes to define relative motivic complexes for a smooth, formal lifting of Y_m over $W(W_m(k))$.

Speaker: Tomoki Mihara

Title: On Schikhof Dual of p -adic Formal Groups

Abstract: I introduce dualities between profinite Abelian groups and certain Abelian formal groups and between discrete groups and certain analytic groups over local fields as non-Archimedean analogues of Pontryagin duality. Extending the dualities, I study Schikhof duality between Hopf monoids in symmetric monoidal categories of linear compact flat modules and of Banach spaces. For example, every formal group forms a Hopf monoid in the former symmetric monoidal category, and its representation, which is a comodule by definition, is presented as a module over the dual Hopf monoid. The dual presentation gives analogues of highest weight theory and the construction of irreducible representations using Groebner bases, and hence is useful to construct a universal p -adic family interpolating irreducible representations. As an application, a p -adic family of Galois representations associated to elliptic modular forms appears in the étale cohomology of the sheaf on a modular curve associated to the universal p -adic family for SL_2 . Moreover, Schikhof dual of quantum groups obtained as deformations of formal groups admit good presentations, and is helpful to study their representations.

Speaker: Jan Nekovář

Title: Some remarks on arithmetic local constants

Abstract: We are going to discuss several compatibility results between arithmetic local constants of Mazur and Rubin and the usual local epsilon constants. These results have applications in a global setting.

Speaker: Shusuke Otabe

Title: On a purely inseparable analogue of the Abhyankar conjecture for affine curves

Abstract: Let U be an affine smooth curve defined over an algebraically closed field of positive characteristic. The Abhyankar conjecture (proved by Raynaud and Harbater in 1994) describes the set of finite quotients of Grothendieck’s étale fundamental group $\pi_1^{\text{ét}}(U)$. In this talk, I will consider a purely inseparable analogue of this problem, formulated in terms of Nori’s profinite fundamental group scheme $\pi^N(U)$. I will state a conjectural description of all the infinitesimal quotients of $\pi^N(U)$ and give several evidences of it.

Speaker: Shun Ohkubo

Title: On the rationality of the logarithmic growth filtration of solutions of p -adic differential equations

Abstract: In his study of p -adic differential equations, B.Dwork proved that the power series solutions of certain p -adic differential equations such as (p -adic) Gaussian hypergeometric one satisfy a mild growth condition. Recently, B.Chiarellotto and N.Tsuzuki reconsidered Dwork’s work and conjectured a relationship between the order of growth and Frobenius slopes of the space of solutions. In this talk, we discuss some part of Chiarellotto-Tsuzuki conjecture.

Speaker: Takeshi Saito

Title: Characteristic cycle of an l -adic sheaf

Abstract: For an l -adic sheaf on a smooth variety over a perfect field, its characteristic cycle is defined as a \mathbb{Z} -linear combination of irreducible components of the singular support, defined by Beilinson as a closed conical subset of the cotangent bundle. It gives an analogue of that defined by Kashiwara-Schapira in a transcendental setting. We discuss its properties, including a recent progress on the compatibility with proper direct image.

Speaker: Atsushi Shiho

Title: Comparison of relatively unipotent log de Rham fundamental groups

Abstract: We prove the compatibilities of various definitions of relatively unipotent log de Rham fundamental groups for certain proper log smooth integral morphisms of fine log schemes of characteristic zero. Our proofs are purely algebraic. As an application, we give a purely algebraic calculation of the monodromy action on the unipotent log de Rham fundamental group of log curves, which enables us to give a purely algebraic proof of the p -adic good reduction criterion for proper hyperbolic curves due to Andreatta-Iovita-Kim. This is a joint work with Bruno Chiarellotto and Valentina Di Proietto.

Speaker: Nobuo Tsuzuki

Title: On constancy of Newton polygons of F -isocrystals on Abelian varieties

Abstract: In this talk we study variation of Newton polygons of F -isocrystals and prove the constancy of them on Abelian varieties. We also discuss the isotriviality of families of curves.

Speaker: Kazuki Yamada

Title: **Category of mixed plectic Hodge structures**

Abstract: Let \mathcal{G} be the tannakian fundamental group of the category of mixed Hodge structures, and fix a positive integer g . In this talk, we will characterize a representation of \mathcal{G}^g in terms of a weight filtration and g partial Hodge filtrations. According to the plectic conjecture of Nekovar and Scholl, such objects would appear in the Hodge realization of motives with real multiplication. This is joint work with Kenichi Bannai, Kei Hagihara, Shinichi Kobayashi, Shuji Yamamoto, and Seidai Yasuda.

Speaker: Shuji Yamamoto

Title: Kawashima functions and multiple zeta values

Abstract: The Kawashima functions, which are introduced and applied to the study of multiple zeta values by Gaku Kawashima, can be viewed as ‘multiplication’ of the digamma function. In this talk, I show how some analytic formulas on the digamma function are generalized to the Kawashima functions, and how they can be used to obtain algebraic relations among multiple zeta values. If time permits, I also present some unsolved questions.

Speaker: Jeng-Daw Yu

Title: Recent developments in irregular Hodge filtrations

Abstract: The existence of a Hodge type filtration on certain connections with irregular singularities was suggested by the considerations of Landau-Ginzburg models in mirror symmetry and the analogies with wild ramifications in étale sheaves in positive characteristic. In this talk, we report some recent results on the constructions of the irregular Hodge filtrations and focus on the structures of the resulting objects over a low dimensional base, e.g., the tensor product structure when the base is a point. Based on collaborations with Claude Sabbah.